How to Win the Clone Wars: Efficient Periodic n-Times Anonymous Authentication

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ABSTRACT

We create a credential system that lets a user anonymously authenticate at most n times in a single time period. A user withdraws a dispenser of n e-tokens. She shows an etoken to a verifier to authenticate herself; each e-token can be used only once, however, the dispenser automatically refreshes every time period. The only prior solution to this problem, due to Damgård et al. [29], uses protocols that are a factor of k slower for the user and verifier, where kis the security parameter. Damgård et al. also only support one authentication per time period, while we support n. Because our construction is based on e-cash, we can use existing techniques to identify a cheating user, trace all of her e-tokens, and revoke her dispensers. We also offer a new anonymity service: glitch protection for basically honest users who (occasionally) reuse e-tokens. The verifier can always recognize a reused e-token; however, we preserve the anonymity of users who do not reuse e-tokens too often.

Categories and Subject Descriptors: K.6.5 [Security and Protection]:Authentication.

General Terms: Security, Algorithms.

Keywords: n-anonymous authentication, clone detection, credentials.

1. INTRODUCTION

As computer devices get smaller and less intrusive, it becomes possible to place them everywhere and use them to collect information about their environment. For example, with today's technology, sensors mounted on vehicles may report to a central traffic service which parts of the roads are treacherous, thus assisting people in planning their commutes. Some have proposed mounting sensors in refrigerators to report the consumption statistics of a household, thus aiding in public health studies, or even mounting them in people's bodies in an attempt to aid medical science. In all these areas, better information may ultimately lead to a better quality of life.

Yet this vision appears to be incompatible with privacy. A sensor installed in a particular car will divulge that car's location, while one installed in a fridge will report the eating and drinking habits of its owner.

A naive solution would be to supply only the relevant information and nothing else.¹ A report about the road conditions should not say which sensor made the measurement. However, then nothing would stop a malicious party from supplying lots of false and misleading data. We need to authenticate the information reported by a sensor without divulging the sensor's identity. We also need a way to deal with rogue sensors, i.e., formerly honest sensors with valid cryptographic keys that are captured by a malicious adversary and used to send lots of misleading data.

The same problem arises in other scenarios. Consider an interactive computer game. Each player must have a license to participate, and prove this fact to an on-line authority every time she wishes to play. For privacy reasons, the player does not wish to reveal anything other than the fact that she has a license. How can we prevent a million users from playing the game for the price of just one license?

A suite of cryptographic primitives such as group signatures [27, 21, 1, 6] and anonymous credentials [25, 30, 39, 14, 16, 17] has been developed to let us prove that a piece of data comes from an authorized source without revealing the identity of that particular source. However, none of the results cited above provide a way to ensure anonymity and unlinkability of honest participants while at the same time guaranteeing that a rogue cannot undetectably provide misleading data in bulk. Indeed, it seems that the ability to provide false data is a consequence of anonymity.

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¹Divulging the relevant information alone may already constitute a breach of privacy. This has to do with statistical properties of the data itself. See Sweeney [46] and Chawla et al. [28] on the challenges of determining which data is and is not safe to reveal.

Recently Damgård, Dupont and Pedersen [29] presented a scheme that overcomes this seeming paradox. The goal is to allow an honest participant to anonymously and unlinkably submit data at a small rate (for example, reporting on road conditions once every fifteen minutes, or joining one game session every half an hour), and at the same time to have a way to identify participants that submit data more frequently. This limits the amount of false information a rogue sensor can provide or the number of times that a given software license can be used per time period.

While the work of Damgård et al. is the first step in the right direction, their approach yields a prohibitively expensive solution. To authenticate itself, a sensor acts as a prover in a zero-knowledge (ZK) proof of knowledge of a relevant certificate. In their construction, the zero-knowledge property crucially depends on the fact that the prover must make some random choices; should the prover ever re-use the random choices he made, the prover's secrets can be efficiently computed from the two transcripts. The sensor's random choices are a pseudorandom function of the current time period (which must be proven in an additional ZK proof protocol). If a rogue sensor tries to submit more data in the same time period, he will have to use the same randomness in the proof, thus exposing his identity. It is very challenging to instantiate this solution with efficient building blocks. Damgård et al. use the most efficient building blocks available, and also introduce some of their own; their scheme requires that the user perform 57+68k exponentiations to authenticate, where k is the security parameter (a sensor can cheat with probability 2^{-k}).

We provide a completely different approach that yields a practical, efficient, and provably secure solution. We relate the problem to electronic cash (e-cash) [23, 24] and in particular, to compact e-cash [12]. In our approach, each participant obtains a set of e-tokens from the central server. Similar to the withdrawal protocol of e-cash, the protocol through which a participant obtains these e-tokens does not reveal any information to the server about what these etokens actually look like. Our protocol lets a participant obtain all the e-tokens it will ever need in its lifetime in one efficient transaction. The user performs only 3 multi-base exponentiations to obtain e-tokens, and 35 multi-base exponentiations to show a single e-token. If the user is limited to one e-token per time period (as in the Damgård et al.'s scheme), the scheme can be further simplified and the user will need to do only 13 multi-base exponentiations to show an e-token. We provide more details on efficiency in §4.3.

Distributed sensors can use an e-token to anonymously authenticate the data they send to the central server. In the on-line game scenario, each e-token can be used to establish a new connection to the game. Unlike e-cash, where it is crucial to limit the amount of money withdrawn in each transaction, the number of e-tokens obtained by a participant is unlimited, and a participant can go on sending data or connecting to the game for as long as it needs. The e-tokens are anonymous and unlinkable to each other and to the protocol where they were obtained. However, the number of e-tokens that are valid during a particular time period *is* limited. Similarly to what happens in compact ecash, reusing e-tokens leads to the identification of the rogue participant. We also show how to reveal all of its past and future transactions.

Thus, in the sensor scenario, a sensor cannot send more

than a small number of data items per time period, so there is a limit to the amount of misleading data that a rogue sensor can submit. Should a rogue sensor attempt to do more, it will have to reuse some of its e-tokens, which will lead to the identification of itself and possibly all of its past and future transactions. Similarly, in the on-line game scenario, a license cannot be used more than a small number of times per day, and so it is impossible to share it widely.

OUR CONTRIBUTION Our main contribution is the new approach to the problem, described above, that is an order of magnitude more efficient than the solution of Damgård et al. In Section 4, we present our basic construction, which is based on previously-proposed complexity theoretic assumptions (SRSA and y-DDHI) and is secure in the plain model.

Our construction builds on prior work on anonymous credentials [14, 38], so that it is easy to see which parts need to be slightly modified, using standard techniques, to add additional features such as an anonymity revoking trustee, identity attributes, etc. The computational cost of these additional features is a few additional modular exponentiations per transaction.

In Section 5, we extend our basic solution to make it tolerate occasional glitches without disastrous consequences to the anonymity of a participant. Suppose that a sensor gets reset and does not realize that it has already sent in a measurement. This should not necessarily invalidate all of the sensor's data. It is sufficient for the data collection center to notice that it received two measurements from the same sensor, and act accordingly. It is, of course, desirable, that a sensor that has too many such glitches be discovered and replaced. Our solution allows us to be flexible in this respect, and tolerates m such glitches (where m is specified ahead of time as a system-wide parameter) at the additive cost of O(km) in both efficiency and storage, where k is the security parameter. This does not add any extra computational or set-up assumptions to our basic scheme.

In Section 6, we consider more variations of our basic scheme. We show, also in the plain model, how to enable the issuer and verifiers to prove to third parties that a particular user has (excessively) reused e-tokens (this is called *weak exculpability*); and enable the issuer and verifiers to trace all e-tokens from the same dispenser as the one that was excessively reused (this is called *tracing*). We also show, in the common-parameters and random-oracle models, how to achieve *strong exculpability*, where the honest verifiers can prove to third parties that a user reused a particular e-token. Finally, we explain how e-token dispensers can be revoked; this requires a model where the revocation authority can continuously update the issuer's public key.

A NOTE ON TERMINOLOGY Damgård et al. call the problem at hand "unclonable group identification," meaning that, should a user make a copy of his sensor, the existence of such a clone will manifest itself when both sensors try to submit a piece of data in the same time period. We extend the problem, and call the extended version "periodic *n*-times anonymous authentication," because it is a technique that allows one to provide anonymous authentication up to *n* times during a given time period. For n = 1 (when there is only one e-token per user per time period) our scheme solves the same problem as the Damgård et al. scheme.

RELATED WORK Anonymity, conditional anonymity, and revocable anonymity, are heavily researched fields; due to space constraints, we compare ourselves only to the most relevant and the most recent work. Anonymous credentials allow one to prove that one has a set of credentials without revealing anything other than this fact. Revocable anonymity [27, 10, 18, 37] allows a trusted third party to discover the identity of all otherwise anonymous participants; it is not directly relevant to our efforts since we do not assume any such TTP, nor do we want anyone to discover the identity of honest users. Conditional anonymity requires that a user's transactions remain anonymous until some conditions are violated; our results fall within that category. With the exception of Damgård et al.'s work [29], no prior literature on conditional anonymity considered conditions of the form "at most n anonymous transactions per time period are allowed." Most prior work on conditional anonymity focused on e-cash [26, 9, 12], where the identity of double-spenders could be discovered. A recent variation on the theme is Jarecki and Shmatikov's [36] work on anonymous, but linkable, authentication where one's identity can be discovered after one carries out too many transactions. Another set of recent papers [47, 42] addressed a related problem of allowing a user to show a credential anonymously and unlinkably up to k times. Showing an anonymous credential more than k times allows a verifier to link the k + 1 st showing to a previous transaction, but, in contrast to our scheme, does not in any way lead to the identification of the misbehaving user.

2. DEFINITION OF SECURITY

Our definitions for periodic *n*-times anonymous authentication are based on the e-cash definitions of [12] and [13]. We define a scheme where users \mathcal{U} obtain e-token dispensers from the issuer \mathcal{I} , and each dispenser can dispense up to *n* anonymous and unlinkable e-tokens per time period, but no more; these e-tokens are then given to verifiers \mathcal{V} that guard access to a resource that requires authentication (e.g., an on-line game). \mathcal{U} , \mathcal{V} , and \mathcal{I} interact using the following algorithms:

- IKeygen $(1^k, params)$ is the key generation algorithm of the e-token issuer \mathcal{I} . It takes as input 1^k and, if the scheme is in the common parameters model, these parameters params. It outputs a key pair $(pk_{\mathcal{I}}, sk_{\mathcal{I}})$. Assume that params are appended as part of $pk_{\mathcal{I}}$ and $sk_{\mathcal{I}}$.
- UKeygen $(1^k, pk_{\mathcal{I}})$ creates the user's key pair $(pk_{\mathcal{U}}, sk_{\mathcal{U}})$ analogously.
- Obtain($\mathcal{U}(pk_{\mathcal{I}}, sk_{\mathcal{U}}, n), \mathcal{I}(pk_{\mathcal{U}}, sk_{\mathcal{I}}, n)$) At the end of this protocol, the user obtains an e-token dispenser D, usable n times per time period and (optionally) the issuer obtains tracing information t_D and revocation information r_D . \mathcal{I} adds t_D and r_D to a record $R_{\mathcal{U}}$ which is stored together with $pk_{\mathcal{U}}$.
- Show($\mathcal{U}(D, pk_{\mathcal{I}}, t, n), \mathcal{V}(pk_{\mathcal{I}}, t, n)$). Shows an e-token from dispenser D in time period t. The verifier outputs a token serial number (TSN) S and a transcript τ . The user's output is an updated e-token dispenser D'.
- Identify $(pk_{\mathcal{I}}, S, \tau, \tau')$. Given two records (S, τ) and (S, τ') output by honest verifiers in the Show protocol, where $\tau \neq \tau'$, computes a value $s_{\mathcal{U}}$ that can identify the owner of the dispenser D that generated TSN S.

The value $s_{\mathcal{U}}$ may also contain additional information specific to the owner of D that (a) will convince third parties that \mathcal{U} is a violator (weak exculpability), that (b) will convince third parties that \mathcal{U} double-showed this e-token (strong exculpability), or that (c) can be used to extract all token serial numbers of \mathcal{U} (traceability).

A periodic *n*-times anonymous authentication scheme needs to fulfill the following three properties:

Soundness. Given an honest issuer, a set of honest verifiers are guaranteed that, collectively, they will not have to accept more than n e-tokens from a single e-token dispenser in a single time period. There is a knowledge extractor \mathcal{E} that executes u Obtain protocols with all adversarial users and produces functions, f_1, \ldots, f_u , with $f_i : \mathbb{T} \times \mathbb{I} \to \mathbb{S}$. I is the index set [0.n-1], \mathbb{T} is the domain of the time period identifiers, and \mathbb{S} is the domain of TSN's. Running though all $j \in \mathbb{I}$, $f_i(t, j)$ produces all n TSNs for dispenser i at time $t \in \mathbb{T}$. We require that for every adversary, the probability that an honest verifier will accept S as a TSN of a Show protocol executed in time period t, where $S \neq f_i(j,t), \forall 1 \leq i \leq u$ and $\forall 0 \leq j < n$ is negligible.

Identification. There exists an efficient function ϕ with the following property. Suppose the issuer and verifiers $\mathcal{V}_1, \mathcal{V}_2$ are honest. If \mathcal{V}_1 outputs (S, τ) and \mathcal{V}_2 outputs (S, τ') as the result of Show protocols, then $\mathsf{Identify}(pk_{\mathcal{I}}, S, \tau, \tau')$ outputs a value $s_{\mathcal{U}}$, such that $\phi(s_{\mathcal{U}}) = pk_{\mathcal{U}}$, the violator's public key. In the sequel, when we say that a user has reused an e-token, we mean that there exist $(S, \tau) (S, \tau')$ that are both output by honest verifiers.

Anonymity. This property is captured as follows: the adversary, acting as the issuer, may run many Obtain protocols with many honest users. Then this adversary may invoke Show protocols with users of his choice, up to n times per time period with the same user. The adversary should not be able to distinguish whether he is indeed interacting with real users or with a simulator S that pretends to be real users without knowing anything about them, including which users it is supposed to be at any point in time, and without access to any secret or public key, or the user's e-token dispenser D. A formal definition for anonymity appears in the full version of this paper.

Additional Extensions In $\S5$, we provide definitions of security in the context of *glitches*, i.e., re-use of e-tokens that do not occur "too often."

In §6, we discuss natural extensions to our basic construction that build on prior work on anonymous credentials and e-cash, namely the concepts of weak and strong exculpability, tracing, and revocation. We now define the corresponding algorithms and security guarantees for these extensions:

- VerifyViolator $(pk_{\mathcal{I}}, pk_{\mathcal{U}}, s_{\mathcal{U}})$ publicly verifies that the user with public key $pk_{\mathcal{U}}$ has double-spent at least one e-token.
- VerifyViolation $(pk_{\mathcal{I}}, S, pk_{\mathcal{U}}, s_{\mathcal{U}})$ publicly verifies that the user with public key $pk_{\mathcal{U}}$ is guilty of double-spending the e-token with TSN S.
- Trace $(pk_{\mathcal{I}}, pk_{\mathcal{U}}, s_{\mathcal{U}}, R_{\mathcal{U}}, n)$, given a valid proof $s_{\mathcal{U}}$ and the user's tracing record $R_{\mathcal{U}}$, computes all TSNs corresponding to this user. Suppose the user has obtained u e-token dispensers, Trace outputs functions f_1, \ldots, f_u such that by running though all $j \in [0..n-1]$, $f_i(t,j)$ produces all n TSNs for e-token dispenser D_i at time t. If $s_{\mathcal{U}}$ is invalid, i.e. VerifyViolator $(pk_{\mathcal{I}}, pk_{\mathcal{U}}, s_{\mathcal{U}})$ rejects, Trace does nothing.

- Revoke $(pk_{\mathcal{I}}, r_D, RD)$ takes as input a revocation database RD (initially empty) and revocation information r_D that corresponds to a particular user (see Obtain). It outputs the updated revocation database RD. In the sequel, we assume that RD is part of $pk_{\mathcal{I}}$.

These algorithms should fulfill the following properties:

Weak exculpability. An adversary cannot successfully blame an honest user \mathcal{U} for reusing an e-token. More specifically, suppose an adversary can adaptively direct a user \mathcal{U} to obtain any number of dispensers and show up to n e-tokens per dispenser per time period. The probability that the adversary produces $s_{\mathcal{U}}$ such that VerifyViolator($pk_{\mathcal{I}}, pk_{\mathcal{U}}, s_{\mathcal{U}}$) accepts is negligible.

Strong exculpability. An adversary cannot successfully blame a user \mathcal{U} of reusing an e-token with token serial number S, even if \mathcal{U} double-showed some other e-tokens. More specifically, suppose an adversary can adaptively direct a user to obtain any number of dispensers and show any number of e-tokens per dispenser per time period (i.e. he can reset the dispenser's state so that the dispenser reuses some of its etokens). The probability that the adversary outputs a token serial number S that was not reused and a proof $s_{\mathcal{U}}$ such that VerifyViolation($pk_{\mathcal{I}}, S, pk_{\mathcal{U}}, s_{\mathcal{U}}$) accepts is negligible.

Tracing of violators. The token serial numbers of violators can be efficiently computed. More specifically, given a value $s_{\mathcal{U}}$ such that VerifyViolator $(pk_{\mathcal{I}}, pk_{\mathcal{U}}, s_{\mathcal{U}}, n)$ accepts, and supposing \mathcal{U} has obtained u e-token dispensers, Trace $(pk_{\mathcal{I}}, pk_{\mathcal{U}}, s_{\mathcal{U}}, R_{\mathcal{U}}, n)$ produces functions f_1, \ldots, f_u such that by running though all $j \in [0..n - 1], f_i(t, j)$ produces all n TSNs for e-token dispenser i at time t.

Dynamic revocation. The Show protocol will only succeed for dispensers D that have not been revoked with Revoke. (Recall that Show takes as input the value $pk_{\mathcal{I}}$ that contains the database DB of revoked users.)

3. PRELIMINARIES

Our e-token system can be shown secure under several different complexity assumptions. Notation: we write $\mathbb{G} = \langle g \rangle$ to denote that g generates the group \mathbb{G} .

BILINEAR MAPS. Let Bilinear_Setup be an algorithm that, on input the security parameter 1^k , outputs the parameters for a bilinear map as $\gamma = (q, g_1, h_1, \mathbb{G}_1, g_2, h_2, \mathbb{G}_2, \mathbb{G}_T, \mathbf{e})$. Each group $\mathbb{G}_1 = \langle g_1 \rangle = \langle h_1 \rangle$, $\mathbb{G}_2 = \langle g_2 \rangle = \langle h_2 \rangle$, and \mathbb{G}_T are of prime order $q \in \Theta(2^k)$. The efficient mapping $\mathbf{e} :$ $\mathbb{G}_1 \times \mathbb{G}_2 \to \mathbb{G}_T$ is both: (*Bilinear*) for all $g_1 \in \mathbb{G}_1, g_2 \in \mathbb{G}_2$, and $a, b \in \mathbb{Z}_q^2, \mathbf{e}(g_1^a, g_2^b) = \mathbf{e}(g_1, g_2)^{ab}$; and (*Non-degenerate*) if g_1 is a generator of \mathbb{G}_1 and g_2 is a generator of \mathbb{G}_2 , then $\mathbf{e}(g_1, g_2)$ generates \mathbb{G}_T .

COMPLEXITY ASSUMPTIONS. The security of our scheme relies on the following assumptions:

Strong RSA Assumption [4, 34]: Given an RSA modulus n and a random element $g \in \mathbb{Z}_n^*$, it is hard to compute $h \in \mathbb{Z}_n^*$ and integer e > 1 such that $h^e \equiv g \mod n$. The modulus n is of a special form pq, where p = 2p' + 1 and q = 2q' + 1 are safe primes.

Additionally, our constructions require *one* of y-DDHI or SDDHI, depending on the size of the system parameters. Alternatively, we can substitute DDH for either of these

assumptions, where the cost is an increase in our time and space complexity by a factor roughly the security parameter. *y*-Decisional Diffie-Hellman Inversion (*y*-DDHI) [5, 32]: Suppose that $g \in \mathbb{G}$ is a random generator of order $q \in \Theta(2^k)$. Then, for all probabilistic polynomial time adversaries \mathcal{A} ,

$$\Pr[a \leftarrow \mathbb{Z}_q^*; \ x_0 = g^{1/a}; \ x_1 \leftarrow \mathbb{G}; \ b \leftarrow \{0, 1\}; \\ b' \leftarrow \mathcal{A}(g, g^a, g^{a^2}, \dots, g^{a^y}, x_b) : b = b'] < 1/2 + 1/\text{poly}(k).$$

In the full version of this paper, we show that the SDDHI assumption holds in generic groups.

Strong DDH Inversion (SDDHI): Suppose that $g \in \mathbb{G}$ is a random generator of order $q \in \Theta(2^k)$. Let $\mathcal{O}_a(\cdot)$ be an oracle that, on input $z \in \mathbb{Z}_q^*$, outputs $g^{1/(a+z)}$. Then, for all probabilistic polynomial time adversaries $\mathcal{A}^{(\cdot)}$ that do not query the oracle on x,

$$\Pr[a \leftarrow \mathbb{Z}_q^*; \ (x, \alpha) \leftarrow \mathcal{A}^{\mathcal{O}_a}(g, g^a); \ y_0 = g^{1/(a+x)}; \ y_1 \leftarrow \mathbb{G};$$
$$b \leftarrow \{0, 1\}; \ b' \leftarrow \mathcal{A}^{\mathcal{O}_a}(y_b, \alpha) : b = b'] < 1/2 + 1/\operatorname{poly}(k).$$

Additionally, our constructions require *one* of the following assumptions. XDH requires non-supersingular curves, whereas SF-DDH may reasonably be conjectured to hold in any bilinear group.

External Diffie-Hellman Assumption (XDH) [35, 44, 40, 6, 3]: Suppose Bilinear_Setup (1^k) produces the parameters for a bilinear mapping $\mathbf{e} : \mathbb{G}_1 \times \mathbb{G}_2 \to \mathbb{G}_T$. The XDH assumption states that the Decisional Diffie-Hellman (DDH) problem is hard in \mathbb{G}_1 .

Sum-Free Decisional Diffie-Hellman Assumption (SF-DDH) [31]: Suppose that $g \in \mathbb{G}$ is a random generator of order $q \in \Theta(2^k)$. Let L be any polynomial function of k. Let $\mathcal{O}_{\vec{a}}(\cdot)$ be an oracle that, on input a subset $I \subseteq \{1, \ldots, L\}$, outputs the value $g_1^{\beta_I}$ where $\beta_I = \prod_{i \in I} a_i$ for some $\vec{a} = (a_1, \ldots, a_L) \in \mathbb{Z}_q^L$. Further, let R be a predicate such that $R(J, I_1, \ldots, I_t) = 1$ if and only if $J \subseteq \{1, \ldots, L\}$ is DDHindependent from the I_i 's; that is, when $v(I_i)$ is the L-length vector with a one in position j if and only if $j \in I_i$ and zero otherwise, then there are no three sets I_a, I_b, I_c such that $v(J) + v(I_a) = v(I_b) + v(I_c)$ (where addition is bitwise over the integers). Then, for all probabilistic polynomial time adversaries $\mathcal{A}^{(\cdot)}$,

$$\Pr[\vec{a} = (a_1, \dots, a_L) \leftarrow \mathbb{Z}_q^L; (J, \alpha) \leftarrow \mathcal{A}^{\mathcal{O}_{\vec{a}}}(1^k); y_0 = g^{\prod_{i \in J} a_i};$$
$$y_1 \leftarrow \mathbb{G}; b \leftarrow \{0, 1\}; b' \leftarrow \mathcal{A}^{\mathcal{O}_{\vec{a}}}(y_b, \alpha) : b = b' \land$$
$$R(J, Q) = 1] < 1/2 + 1/\operatorname{poly}(k),$$

where Q is the set of queries that \mathcal{A} made to $\mathcal{O}_{\vec{a}}(\cdot)$.

KEY BUILDING BLOCKS. We summarize the necessary information about our system components.

DY Pseudorandom Function (PRF). Let $\mathbb{G} = \langle g \rangle$ be a group of prime order $q \in \Theta(2^k)$. Let *a* be a random element of \mathbb{Z}_q^* . Dodis and Yampolskiy [32] showed that $f_{g,a}^{DY}(x) = g^{1/(a+x)}$ is a pseudorandom function, under the *y*-DDHI assumption, when either: (1) the inputs are drawn from the restricted domain $\{0, 1\}^{O(\log k)}$ only, or (2) the adversary specifies a polynomial-sized set of inputs from \mathbb{Z}_q^* before a function is selected from the PRF family (i.e., before the value *a* is selected). For our purposes, we require something stronger: that the DY construction work for inputs drawn arbitrarily and adaptively from \mathbb{Z}_q^* . THEOREM 3.1. In the generic group model, the Dodis-Yampolskiy PRF is adaptively secure for inputs in \mathbb{Z}_q^* .

The proof is included in the full version of this paper.

Pedersen and Fujisaki-Okamoto Commitments. Recall the Pedersen commitment scheme [43], in which the public parameters are a group \mathbb{G} of prime order q, and generators (g_0, \ldots, g_m) . In order to commit to the values $(v_1, \ldots, v_m) \in \mathbb{Z}_q^m$, pick a random $r \in \mathbb{Z}_q$ and set $C = \operatorname{PedCom}(v_1, \ldots, v_m; r) = g_0^r \prod_{i=1}^m g_i^{v_i}$.

Fujisaki and Okamoto [34] showed how to expand this scheme to composite order groups.

CL Signatures. Camenisch and Lysyanskaya [16] came up with a secure signature scheme with two protocols: (1) An efficient protocol for a user to obtain a signature on the value in a Pedersen (or Fujisaki-Okamoto) commitment [43, 34] without the signer learning anything about the message. (2) An efficient proof of knowledge of a signature protocol. Security is based on the Strong RSA assumption. Using bilinear maps, we can use other signature schemes [17, 6] for shorter signatures.

Verifiable Encryption. For our purposes, in a verifiable encryption scheme, the encrypter/prover convinces a verifier that the plaintext of an encryption under a known public key is equivalent to the value hidden in a Pedersen commitment.

Camenisch and Damgård [11] developed a technique for turning any semantically-secure encryption scheme into a verifiable encryption scheme.

Bilinear El Gamal Encryption. We require a cryptosystem where g^x is sufficient for decryption and the public key is $\phi(g^x)$ for some function ϕ . One example is the bilinear El Gamal cryptosystem [7, 2], which is semantically secure under the DBDH assumption; that is, given (g, g^a, g^b, g^c, Q) , it is difficult to decide if $Q = \mathbf{e}(g, g)^{abc}$. DBDH is implied by *y*-DDHI or Sum-Free DDH.

AGREEING ON THE TIME. Something as natural as time becomes a complex issue when it is part of a security system. First, it is necessary that the time period t be the same for all users that show e-tokens in that period. Secondly, it should be used only for a single period, i.e., it must be unique. Our construction in §4 allows for the use of arbitrary time period identifiers, such as those negotiated using the hash tree protocol in [29]. For Glitch protection, §5, we assume a totally ordered set of time period identifiers.

4. A PERIODIC *N*-TIMES ANONYMOUS AUTHENTICATION SCHEME

4.1 Intuition Behind our Construction

In a nutshell, the issuer and the user both have key pairs. Let the user's keypair be $(pk_{\mathcal{U}}, sk_{\mathcal{U}})$, where $pk_{\mathcal{U}} = g^{sk_{\mathcal{U}}}$ and g is a generator of some group G of known order. Let f_s be a pseudorandom function whose range is the group G. During the **Obtain** protocol, the user obtains an e-token dispenser D that allows her to show up to n tokens per time period. The dispenser D is comprised of seed s for PRF f_s , the user's secret key $sk_{\mathcal{U}}$, and the issuer's signature on $(s, sk_{\mathcal{U}})$. We use CL signatures to prevent the issuer from learning anything about s or $sk_{\mathcal{U}}$. In the **Show** protocol, the user shows her i^{th} token in time period t: she releases TSN $S = f_s(0, t, i)$, a double-show tag $E = pk_{\mathcal{U}} \cdot f_s(1, t, i)^R$ (for a random R supplied by the verifier), and runs a ZK proof protocol that (S, E) correspond to a valid dispenser for time period t and $0 \leq i < n$ (the user proves that S and E were properly formed from values $(s, sk_{\mathcal{U}})$ signed by the issuer). Since f_s is a PRF, and all the proof protocols are zero-knowledge, it is computationally infeasible to link the resulting e-token to the user, the dispenser D, or any other e-tokens corresponding to D. If a user shows n + 1 e-tokens during the same time interval, then two of the e-tokens must use the same TSN. The issuer can easily detect the violation and compute $pk_{\mathcal{U}}$ from the two double-show tags, $E = pk_{\mathcal{U}} \cdot f_s(1,t,i)^R$ and $E' = pk_{\mathcal{U}} \cdot f_s(1,t,i)^{R'}$. From the equations above, $f_s(1,t,i) = (E/E')^{(R-R')^{-1}}$ and $pk_{\mathcal{U}} = E/f_s(1,t,i)^R$.

4.2 Our Basic Construction

Let k be a security parameter and $l_q \in O(k)$, l_x , l_{time} , and l_{cnt} be system parameters such that $l_q \ge l_x > l_{\text{time}} + l_{\text{cnt}} + 3$ and $2^{l_{\text{cnt}}} - 1 > n$, where n is the number of tokens we allow per time period.

In the following, we assume implicit conversion between binary strings and integers, e.g., between $\{0,1\}^l$ and $[0,2^l-1]$. Let $F_{(g,s)}(x) := f_{g,s}^{DY}(x) := g^{1/(s+x)}$ for $x, s \in \mathbb{Z}_q^*$ and $\langle g \rangle = \mathbb{G}$ being of prime order q. For suitably defined l_{time} , l_{cnt} , and l_x define the function $c : \{0,1\}^{l_x - l_{\text{time}} - l_{\text{cnt}}} \times \{0,1\}^{l_{\text{time}}} \times \{0,1\}^{l_{\text{cnt}}} \to \{0,1\}^{l_x}$ as:

$$c(u,v,z) := \left(u 2^{l_{\text{time}}} + v \right) 2^{l_{\text{cnt}}} + z \ .$$

Issuer Key Generation: In $\mathsf{IKeygen}(1^k, params)$, the issuer \mathcal{I} generates two cyclic groups:

- 1. A group $\langle \mathbf{g} \rangle = \langle \mathbf{h} \rangle = \mathbf{G}$ of composite order $\mathbf{p}'\mathbf{q}'$ that can be realized by the multiplicative group of quadratic residue modulo a special RSA modulus $N = (2\mathbf{p}' + 1)(2\mathbf{q}' + 1)$. In addition to CL signatures, this group will be needed for zero-knowledge proofs of knowledge used in the sequel. Note that soundness of these proof systems is computational only and assumes that the prover does not know the order of the group.
- 2. A group $\langle g \rangle = \langle \tilde{g} \rangle = \langle h \rangle = \mathbb{G}$ of prime order q with $2^{l_q-1} < q < 2^{l_q}$.

The issuer must also prove in zero-knowledge that N is a special RSA modulus, and $\langle \mathbf{g} \rangle = \langle \mathbf{h} \rangle$ are quadratic residues modulo N. In the random oracle model, one non-interactive proof may be provided. In the plain model, the issuer must agree to interactively prove this to anyone upon request.

Furthermore, the issuer generates a CL signature key pair (pk, sk) set in group **G**. The issuer's public-key will contain $(\mathbf{g}, \mathbf{h}, \mathbf{G}, g, \tilde{g}, h, \mathbb{G}, pk)$, while the secret-key will contain all of the information.

User Key Generation: In UKeygen $(1^k, pk_{\mathcal{I}})$, the user chooses a random $sk_{\mathcal{U}} \in \mathbb{Z}_q$ and sets $pk_{\mathcal{U}} = g^{sk_{\mathcal{U}}} \in \mathbb{G}$.

Get e-Token Dispenser: Obtain($\mathcal{U}(pk_{\mathcal{I}}, sk_{\mathcal{U}}, n)$, $\mathcal{I}(pk_{\mathcal{U}}, sk_{\mathcal{I}}, n)$). Assume that \mathcal{U} and \mathcal{I} have mutually authenticated. A user \mathcal{U} obtains an e-token dispenser from an issuer \mathcal{I} as follows:

1. \mathcal{U} and \mathcal{I} agree on a commitment C to a random value $s \in \mathbb{Z}_q$ as follows:

- (a) \mathcal{U} selects s' at random from \mathbb{Z}_q and computes $C' = \operatorname{PedCom}(sk_{\mathcal{U}}, s'; r) = q^{sk_{\mathcal{U}}} \tilde{q}^{s'} h^r.$
- (b) \mathcal{U} sends C' to \mathcal{I} and proves that it is constructed correctly.
- (c) \mathcal{I} sends a random r' from \mathbb{Z}_q back to \mathcal{U} .
- (d) Both \mathcal{U} and \mathcal{I} compute $C = C'\tilde{g}^{r'} = \operatorname{PedCom}(sk_{\mathcal{U}}, s' + r'; r)$. \mathcal{U} computes $s = s' + r' \mod q$.
- 2. \mathcal{I} and \mathcal{U} execute the CL signing protocol on commitment C. Upon success, \mathcal{U} obtains σ , the issuer's signature on $(sk_{\mathcal{U}}, s)$. This step can be efficiently realized using the CL protocols [16, 17] in such a way that ${\mathcal I}$ learns nothing about $sk_{\mathcal{U}}$ or s.
- 3. \mathcal{U} initializes counters T := 1 (to track the current period) and J := 0 (to count the e-tokens shown in the current time period). ${\mathcal U}$ stores the e-token dispenser $D = (sk_{\mathcal{U}}, s, \sigma, T, J).$

Use an e-Token: Show($\mathcal{U}(E, pk_{\mathcal{I}}, t, n), \mathcal{V}(pk_{\mathcal{I}}, t, n)$). Let t be the current time period identifier with $0 < t < 2^{l_{\text{time}}}$. (We discuss how two parties might agree on t in Section 3.) A user \mathcal{U} reveals a single e-token from a dispenser D = $(sk_{\mathcal{U}}, s, \sigma, T, J)$ to a verifier \mathcal{V} as follows:

- 1. \mathcal{U} compares t with T. If $t \neq T$, then \mathcal{U} sets T := t and J := 0. If $J \ge n$, abort!
- 2. \mathcal{V} sends to \mathcal{U} a random $R \in \mathbb{Z}_q^*$.
- 3. \mathcal{U} sends to \mathcal{V} a token serial number S and a double spending tag E computed as follows:

$$S = F_{(g,s)}(c(0,T,J)), \qquad E = pk_{\mathcal{U}} \cdot F_{(g,s)}(c(1,T,J))^R$$

- 4. \mathcal{U} and \mathcal{V} engage in a zero-knowledge proof of knowledge of values $sk_{\mathcal{U}}$, s, σ , and J such that:

 - $\begin{array}{ll} \mbox{(a)} & 0 \leq J < n, \\ \mbox{(b)} & S = F_{(g,s)}(c(0,t,J)), \end{array}$

(c)
$$E = g^{sk_{\mathcal{U}}} \cdot F_{(g,s)}(c(1,t,J))^R$$
,

- (d) VerifySig $(pk_{\mathcal{I}}, (sk_{\mathcal{U}}, s), \sigma)$ =true.
- 5. If the proof verifies, \mathcal{V} stores (S, τ) , with $\tau = (E, R)$, in his database. If he is not the only verifier, he also submits this tuple to the database of previously shown e-tokens.
- 6. \mathcal{U} increases counter J by one. If $J \geq n$, the dispenser is empty. It will be refilled in the next time period.

Technical Details. The proof in Step 4 is done as follows:

- 1. \mathcal{U} generates the commitments $C_J = g^J h^{r_1}, C_u =$ $g^{sk_{\mathcal{U}}}h^{r_2}, C_s = g^s h^{r_3}$, and sends them to \mathcal{V} .
- 2. \mathcal{U} proves that C_J is a commitment to a value in the interval [0, n-1] using standard techniques [22, 19, 8].
- 3. \mathcal{U} proves knowledge of a CL signature from \mathcal{I} for the values committed to by C_u and C_s in that order. This step can be efficiently realized using the CL protocols [16, 17].
- 4. \mathcal{U} as prover and \mathcal{V} as verifier engage in the following proof of knowledge, using the notation by Camenisch and Stadler [21]:

$$PK\{(\alpha, \beta, \delta, \gamma_1, \gamma_2, \gamma_3) : g = (C_s g^{c(0,t,0)} C_J)^{\alpha} h^{\gamma_1} \wedge S = g^{\alpha} \wedge g = (C_s g^{c(1,t,0)} C_J)^{\beta} h^{\gamma_2} \wedge C_u = g^{\delta} h^{\gamma_3} \wedge E = g^{\delta} (g^R)^{\beta}\} .$$

 \mathcal{U} proves she knows the values of the Greek letters; all other values are known to both parties.

Let us explain the last proof protocol. From the first step we know that C_J encodes some value \hat{J} with $0 \leq \hat{J} < n$, i.e., $C_J = g^{\hat{J}} h^{\hat{r}_J}$ for some \hat{r}_J . From the second step we know that C_s and C_u encoded some value \hat{u} and \hat{s} on which the prover \mathcal{U} knows a CL signature by the issuer. Therefore, $C_s = g^{\hat{s}} h^{\hat{r}_s}$ and $C_u = g^{\hat{u}} h^{\hat{r}_u}$ for some \hat{r}_s and \hat{r}_u . Next, recall that by definition of $c(\cdot, \cdot, \cdot)$ the term $g^{c(0,t,0)}$ corresponds to $g^{t2^{l_{\text{cnt}}}}$. Now consider the first term $g = (C_s g^{c(0,t,0)} C_J)^{\alpha} h^{\gamma_1}$ in the proof protocol. We can now conclude the prover \mathcal{U} knows values \hat{a} and \hat{r} such that $g = g^{(\hat{s} + t2^{l} \operatorname{cnt} + \hat{J})\hat{a}} h^{\hat{r}}$ and S = $g^{\hat{a}}$. From the first equation is follows that $\hat{a} = (\hat{s} + (t2^{l_{\text{cnt}}} +$ $(\hat{J}))^{-1} \pmod{q}$ must hold provided that \mathcal{U} is not privy to $\log_a h$ (as we show via a reduction in the proof of security) and thus we have established that $S = F_{(g,\hat{s})}(c(0,t,\hat{J}))$ is a valid serial number for the time period t. Similarly one can derive that $E = g^{\hat{u}} \cdot F_{(g,\hat{s})}(c(1,t,\hat{J}))^R$, i.e., that E is a valid double-spending tag for time period t.

Identify Cheaters: $Identify(pk_{\mathcal{I}}, S, (E, R), (E', R'))$. If the verifiers who accepted these tokens were honest, then $R \neq$ R' with high probability, and proof of validity ensures that $E = pk_{\mathcal{U}} \cdot f_s(1,T,J)^R$ and $E' = pk_{\mathcal{U}} \cdot f_s(1,T,J)^{R'}$. The violator's public key can now be computed by first solving for $f_s(1,T,J) = (E/E')^{(R-R')^{-1}}$ and then computing $pk_{\mathcal{U}} = E/f_s(1,T,J)^R$.

THEOREM 4.1. Protocols IKeygen, UKeygen, Obtain, Show, and Identify described above achieve soundness, identification, and anonymity properties in the plain model assuming Strong RSA, and y-DDHI if $l_x \in O(\log k)$ or SDDHI otherwise.

In the full version of this paper, we prove the theorem. Recall that l_x dictates the number of time periods and the number of allowed shows per time period; when these values are small, security is based only on Strong RSA and y-DDHI.

4.3 **Efficiency Discussion**

To analyze the efficiency of our scheme, it is sufficient to consider the number of (multi-base) exponentiations the parties have to do in \mathbb{G} and \mathbf{G} . In a decent implementation, a multi-base exponentiation takes about the same time as a single-base exponentiation, provided that the number of bases is small. For the analysis we assume that the Strong RSA based CL-signature scheme is used.

Obtain: both the user and issuer perform 3 exponentiations in G. Show: the user performs 12 multi-base exponentiation in \mathbb{G} and 23 multi-base exponentiations in \mathbf{G} , while the verifier performs 7 multi-base exponentiation in \mathbb{G} and 13 multi-base exponentiations in **G**. If n is odd, the user only needs to do 12 exponentiations in \mathbf{G} , while the verifier needs to do 7. To compare ourselves to the Damgård et al. [29] scheme, we set n = 1. In this case, Show requires that the user perform 12 multi-base exponentiation in $\mathbb G$ and 1 multi-base exponentiations in $\mathbf G$ and the verifier perform 7 multi-base exponentiation in G and 1 multi-base exponentiations in **G**. Damgård et al. requires 57+68r exponentiations in \mathbb{G} , where r is the security parameter (i.e., 2^{-r} is the probability that the user can cheat). Depending on the application, r should be at least 20 or even 60. Thus, our scheme is an order of magnitude more efficient than Damgård et al.

5. GLITCH PROTECTION EXTENSION

In our periodic *n*-times anonymous authentication scheme, a user who shows two tokens with the same TSN becomes identifiable. (Recall that only *n* unique TSN values are available to a user per time period.) A user might accidentally use the same TSN twice because of hardware breakdowns, clock desychronization, etc. We want to protect the anonymity of users who occasionally cause a *glitch* (repeat a TSN in two different tokens), while still identifying users who cause an excessive amount of glitches. A user might be permitted up to *m* glitches per *monitoring interval* (e.g., year). Any TSN repetition will be detected, but the user's anonymity will not be compromised until the (m+1)st glitch. A token that causes a glitch is called a *clone*.

Suppose a user has u glitches in one monitoring interval. Our goal is to design a scheme where:

- if u = 0, all shows are anonymous and unlinkable;
- if $1 \le u \le m$, all shows remain anonymous, but a link-id L is revealed, making all clones linkable;
- if u > m, the user's public key is revealed.

One can think of link-id L as a pseudonym (per monitoring interval) that is hidden in each token released by the same user (much in the same way that the user's public key was hidden in each token released by a user in the basic scheme). If tokens (S, τ) and (S, τ') caused a glitch, then we call (S, τ, τ') a glitch tuple, where by definition $\tau \neq \tau'$. We introduce a new function GetLinkld that takes as input a glitch tuple and returns the link-id L. Once m + 1 clones are linked to the same pseudoym L, there is enough information from these collective original and cloned transcripts to compute the public key of the user.

We continue to use identifier $t \in \mathbb{T}$ for (indivisible) time periods. Identifier $v \in \mathbb{V}$ refers to a monitoring interval. We give two glitch protection schemes: §5.1 considers disjoint monitoring intervals, while §5.2 works on overlapping monitoring intervals. For the first scheme, we assume the existence of an efficient function $M_{\mathbb{V}}$ that maps every time period t to its unique monitoring interval $v \in \mathbb{V}$.

5.1 Basic Glitch Protection

Our basic glitch protection scheme tolerates up to m clones per monitoring interval v; monitoring intervals are disjoint.

We informally define the protocols and security properties of a periodic authentication scheme with glitch protection:

- ShowGP($\mathcal{U}(D, pk_{\mathcal{I}}, t, n, m), \mathcal{V}(pk_{\mathcal{I}}, t, n, m)$). Shows an e-token from dispenser D in time period t and monitoring interval $v = M_{\mathbb{V}}(t)$. The verifier obtains a token serial number S and a transcript τ .
- GetLinkld($pk_{\mathcal{I}}, S, \tau, \tau'$). Given e-tokens (S, τ, τ') , where $\tau \neq \tau'$ by definition, computes a link-id value L.
- IdentifyGP $(pk_{\mathcal{I}}, (S_1, \tau_1, \tau'_1), \ldots, (S_{m+1}, \tau_{m+1}, \tau'_{m+\ell+1}))$. Given m+1 glitch tuples where for each i, GetLinkld (S_i, τ_i, τ'_i) produces the same link-id L, computes a value $s_{\mathcal{U}}$ that can be used to compute the public key of the owner of the dispenser D from which the TSNs came.

We give two new security properties GP Anonymity and GPIdentification that supercede the Anonymity and Identification properties of §2. *GP* Anonymity. An adversarial issuer, even when cooperating with verifiers and other dishonest users, and adaptively directing honest users to show e-tokens and up to m clones of his choice for every monitoring interval $v \in \mathbb{V}$, cannot learn anything about a user's e-token usage behavior except what is available from side information from the environment. This property is captured by a simulator S which can interact with the adversary as if he were the user. Sdoesn't have access to the user's secret or public key, or her e-token dispenser D. However, when the adversary asks Sto make a clone, the environment passes S a link-id. In the full version of this paper, we provide a formal definition.

GP Identification. Suppose the issuer and verifiers are honest and they receive m + 1 glitch tuples $\mathsf{Input} = (S_1, \tau_1, \tau_1')$, $\ldots, (S_{m+1}, \tau_{m+1}, \tau_{m+1}')$ with the same $L = \mathsf{GetLinkId}(pk_{\mathcal{I}}, S_i, \tau_i, \tau_i')$ for all $1 \leq i \leq m + 1$. Then with high probability algorithm $\mathsf{IdentifyGP}(pk_{\mathcal{I}}, \mathsf{Input})$ outputs a value $s_{\mathcal{U}}$ for which there exists an efficient function ϕ such that $\phi(s_{\mathcal{U}}) = pk_{\mathcal{U}}$, identifying the violator.

Intuition behind construction. Recall that in our basic scheme, an e-token has three logical parts: a serial number $S = F_{(s,g)}(c(0,T,J))$, a tag $E = pk_{\mathcal{U}} \cdot F_{(s,g)}(c(1,T,J))^R$, and a proof of validity. If the user shows a token with TSN S again, then he must reveal $E' = pk_{\mathcal{U}} \cdot F_{(s,g)}(c(1,T,J))^{R'}$, where $R \neq R'$, and the verifier can solve for $pk_{\mathcal{U}}$ from (E, E', R, R').

Now, in our glitch protection scheme, an e-token has four logical parts: a serial number $S = F_{(s,g)}(c(0,T,J))$, a tag K that exposes the link-id L if a glitch occurs, a tag E that exposes $pk_{\mathcal{U}}$ if more than m glitches occur, and a proof of validity.

We instantiate $K = L \cdot F_{(g,s)}(c(2,T,J))^R$. Now a doubleshow reveals L just as it revealed $pk_{\mathcal{U}}$ in the original scheme. The link-id for monitoring interval v is $L = F_{(s,g)}(c(1,v,0))$.

Once the verifiers get m+1 clones with the same link-id L, they need to recover $pk_{\mathcal{U}}$. To allow this, the user includes tag $E = pk_U \cdot \prod_{i=1}^m F_{(g,s)}(c(3,v,i))^{\rho_i} \cdot F_{(s,g)}(c(4,T,J))^R$. (Here, it will be critical for anonymity that the user and the verifier *jointly* choose the random values $R, \rho_1, \ldots, \rho_m$.)

Now, suppose a user causes m + 1 glitches involving ℓ distinct TSNs. Given $(E, R, \rho_1, \ldots, \rho_m)$ from each of these $(m+\ell+1)$ tokens, the public key of the user can be computed by repeatedly using the elimination technique that allowed the discovery of L from (K, K', R, R'). We have $(m+\ell+1)$ equations E and $(m+\ell+1)$ unknown bases including $pk_{\mathcal{U}}$ and the $F_{(s,g)}(.)$ values. Thus, solving for $pk_{\mathcal{U}}$ simply requires solving a system of linear equations.

Construction. ShowGP and IdentifyGP replace the corresponding Show and Identify algorithms of the basic construction in §4.

ShowGP($\mathcal{U}(D, pk_{\mathcal{I}}, t, n, m), \mathcal{V}(pk_{\mathcal{I}}, t, n, m)$). Let $v = M_{\mathbb{V}}(t)$. A user \mathcal{U} shows a single e-token from a dispenser $D = (sk_{\mathcal{U}}, s, \sigma, T, J)$ to a verifier \mathcal{V} as follows:

- 1. \mathcal{U} compares t with T. If t > T, then \mathcal{U} sets T := t and J := 0. If $J \ge n$, abort!
- 2. \mathcal{V} and \mathcal{U} jointly choose $R, \rho_1, \ldots, \rho_m$ uniformly at random from \mathbb{Z}_q^* . The user and verifier can use coinflipping to generate a seed x and then use x to generate the other values (either via a PRF like $F_{g,x}(.)$, or by treating some hash function H(.) as a random oracle).

3. \mathcal{U} sends \mathcal{V} an interval serial number S, a double spending tag K encoding the link-id L, and a special (m+1)cloning tag E:

$$S = F_{(g,s)}(c(0,T,J)),$$

$$K = F_{(g,s)}(c(1,v,0)) \cdot F_{(g,s)}(c(2,T,J))^{R},$$

$$E = pk_{\mathcal{U}} \cdot F_{(g,s)}(c(3,v,1))^{\rho_{1}} \cdots$$

$$F_{(g,s)}(c(3,v,m))^{\rho_{m}} \cdot F_{(g,s)}(c(4,T,J))^{R}$$

- 4. \mathcal{U} performs a zero-knowledge proof that the values above were correctly computed.
- 5. If the proof verifies, \mathcal{V} stores (S, τ) , where $\tau = (K, E, R, \rho_1, \ldots, \rho_m)$, in his database.
- 6. \mathcal{U} increments counter J by one. If $J \ge n$ the dispenser is empty. It will be refilled in the next time period.

GetLinkld $(pk_{\mathcal{I}}, S, (K, E, R, \vec{\rho}), (K', E', R', \vec{\rho'}))$. Returns

$$L = \frac{K}{(K/K')^{(R-R')^{-1}R}}.$$

IdentifyGP $(pk_{\mathcal{I}}, (S_1, \tau_1, \tau'_1), \ldots, (S_{m+1}, \tau_{m+1}, \tau'_{m+1}))$. Let the m+1 glitch tuples include ℓ distinct TSN values. We extract the values $(E_i, R, \rho_1, \ldots, \rho_m)$ (or $(E'_i, R', \rho'_1, \ldots, \rho'_m)$) from all $m + \ell + 1$ unique transcripts. Now, we use the intuition provided above to solve for $pk_{\mathcal{U}}$.

THEOREM 5.1. The scheme described above is a secure periodic n-times anonymous authentication scheme with basic glitch protection. It fulfills the soundness, GP anonymity and GP identification properties.

The proof can be found in the full version of this paper.

5.2 Window Glitch Protection

The basic glitch protection scheme prevents users from creating more than m clones in a single monitoring interval. If two neighboring time periods fall in different monitoring intervals, then a malicious user can create m clones in each of them. We want to catch users who make more than m clones within any W consecutive time periods.

We define an interval of consecutive time-periods to be a window. For convenience, we will consider each time period identifier t to be an integer, and time periods t and t + 1 to be neighbors. Each time period is in W different windows of size W. If we let a time period define the end of a window, then time period t would be in windows $t, t+1, \ldots, t+W-1$.

(m, W)-Window glitch protection allows a user to clone at most m e-tokens during any window of W consecutive time periods. We describe the new protocols associated with a window glitch protection scheme:

- ShowWGP($\mathcal{U}(D, pk_{\mathcal{I}}, t, n, m, W)$, $\mathcal{V}(pk_{\mathcal{I}}, t, n, m, W)$). Shows an e-token from dispenser D for time period t. The verifier obtains a serial number S and a transcript τ .
- GetLinklds $(pk_{\mathcal{I}}, S, \tau, \tau')$. Given two e-tokens (S, τ) and (S, τ') , outputs a *list* of W link-ids L_1, \ldots, L_W .
- IdentifyWGP $(pk_{\mathcal{I}}, (S_1, \tau_1, \tau'_1), \ldots, (S_{m+1}, \tau_{m+1}, \tau'_{m+1}))$. Given m+1 glitch tuples where for each *i*, the same linkid *L* is in the list of link-ids produced by GetLinkld $(S_i, \tau_i,$ $\tau'_i)$, computes a value $s_{\mathcal{U}}$ that can be used to compute the public key of the owner of the dispenser *D* from which the TSNs came.

We modify the *GP Anonymity* and *GP Identification* properties to apply to window glitch protection.

WGP Anonymity. This property is the same as for basic glitch protection, except that now the adversary cannot ask a user to create more than m clones within any window of W consecutive time periods. Since each time period is part of W different windows, the environment will pass the simulator a *set* of link-ids.

WGP Identification. Suppose the issuer and verifiers are honest. Should they receive a list of m + 1 glitch tuples $\mathsf{Input} = (S_1, \tau_1, \tau'_2), \ldots, (S_{m+1}, \tau_{m+1}, \tau'_{m+1})$, such that $\exists L :$ $\forall i : L \in \mathsf{GetLinklds}(pk_{\mathcal{I}}, S_i, \tau_i, \tau'_i)$, then with high probability IdentifyWGP $(pk_{\mathcal{I}}, \mathsf{Input})$ outputs a value $s_{\mathcal{U}}$ for which there exists an efficient function ϕ such that $\phi(s_{\mathcal{U}}) = pk_{\mathcal{U}}$, identifying the violator.

Construction. Intuitively, we replicate our basic glitch solution W times for overlapping windows of W time periods.

ShowWGP($\mathcal{U}(D, pk_{\mathcal{I}}, t, n, m, W)$). We modify the ShowGP protocol as follows. In step 3, the user and verifier jointly choose random numbers R_1, \ldots, R_W and $\rho_{1,1}, \ldots, \rho_{W,m}$. In step 4, the user calculates essentially the same values S, K, E, except that now she calculates separate K_i and E_i tags for every window in which time period T falls:

$$S = F_{(s,g)}(c(0,T,J))$$

$$K_{i} = F_{(s,g)}(c(1,T+i,0)) \cdot F_{(s,g)}(c(2,T,J))^{R_{i}}$$

$$E_{i} = pk_{\mathcal{U}} \cdot F_{(s,g)}(c(3,T+i,1))^{\rho_{i,1}} \cdots$$

$$F_{(s,g)}(c(3,T+i,m))^{\rho_{i,m}} \cdot F_{(s,g)}(c(4,T,J))^{R_{i}}$$

Finally, in step 5, the user proves to the verifier that the values $S, K_1, \ldots, K_W, E_1, \ldots, E_W$ are formed correctly. That, along with the random numbers generated in step 3, forms the transcript stored in steps 6. Step 7 is unchanged.

GetLinklds $(pk_{\mathcal{I}}, S, \tau, \tau')$. Returns the link-ids:

$$L_i = \frac{K_i}{(K_i/K_i')^{(R_i - R_i')^{-1}R_i}}, \quad 1 \le i \le m + 1.$$

IdentifyWGP($pk_{\mathcal{I}}, (S_1, \tau_1, \tau'_2), \ldots, (S_{m+1}, \tau_{m+1}, \tau'_{m+1})$). For all *i*, let $L \in \mathsf{GetLinklds}(pk_{\mathcal{I}}, S_i, \tau_i, \tau'_i)$, that is, let L be the link-id each glitch tuple has in common. Let these m + 1glitch tuples include ℓ distinct TSN values. We extract the values $(E_{i,j}, R_i, \rho_{i,1}, \ldots, \rho_{i,m})$ (or $(E'_{i,j}, R'_i, \rho'_{i,1}, \ldots, \rho'_{i,m})$) from all $m + \ell + 1$ unique transcripts, where *j* depends on where *L* falls in the list $\mathsf{GetLinklds}(pk_{\mathcal{I}}, S_i, \tau_i, \tau'_i)$. Now, we use the same techniques as before to solve for $pk_{\mathcal{U}}$.

THEOREM 5.2. The scheme described above is a secure periodic n-times anonymous authentication scheme with window glitch protection. It fulfills the soundness, WGP anonymity and WGP identification properties.

The proof can be found in the full version of the paper.

6. ADDITIONAL EXTENSIONS

One advantage of our approach to periodic anonymous authentication is that its modular construction fits nicely with previous work [12, 15]. Thus, it is clear which parts of our system can be modified to enable additional features.

6.1 Weak Exculpability

Recall that weak exculpability allows an honest verifier (or group of verifiers) to prove in a sound fashion that the user with public key $pk_{\mathcal{U}}$ reused some token. This convinces everyone in the system that the user with $pk_{\mathcal{U}}$ is untrustworthy.

To implement weak exculpability, we need to define algorithm VerifyViolator and to slightly adapt the IKeygen, UKeygen, Show, and Identify algorithms. IKeygen' now also runs Bilinear_Setup, and the parameters for the bilinear map $\mathbf{e} : \mathbb{G}_1 \times \mathbb{G}_2 \to \mathbb{G}_T$ are added to $pk_{\mathcal{I}}$. UKeygen' selects a random $sk_{\mathcal{U}} \in \mathbb{Z}_q^*$ and outputs $pk_{\mathcal{U}} = \mathbf{e}(g_1, g_2)^{sk_{\mathcal{U}}}$. In the Show' protocol, the double-spending tag is calculated as $E = g_1^{sk_{\mathcal{U}}} \cdot F_{(g_1,s)}(c(1,T,J))^R$. Consequently the value s_U , returned by Identify', is $g_1^{sk_{\mathcal{U}}}$ – which is secret information! Thus, the VerifyViolator algorithm is defined as follows: VerifyViolator($pk_{\mathcal{I}}, pk_{\mathcal{U}}, s_{\mathcal{U}}$) accepts only if $\mathbf{e}(s_{\mathcal{U}}, g_2) = \mathbf{e}(g_1^{sk_{\mathcal{U}}}, g_2) = pk_{\mathcal{U}}$. Intuitively, because $g_1^{sk_{\mathcal{U}}}$ is secret information, its release signals that this user misbehaved.

A subtle technical problem with this approach is that tag E is now set in a bilinear group \mathbb{G}_1 , where DDH may be easy, and we need to ensure that the DY PRF is still secure in this group. Indeed, in groups where DDH is easy, the DY PRF is *not* secure. There are two solutions [12]: (1) make the XDH assumption, i.e., DDH is hard in \mathbb{G}_1 , and continue to use the DY PRF, or (2) make the more general Sum-Free DDH assumption and use the CHL PRF [12], which works in groups where (regular) DDH is easy.

THEOREM 6.1. The above scheme provides weak exculpability under the Strong RSA, y-DDHI if $l_x \in O(\log k)$ or SDDHI, and either XDH or Sum-Free DDH assumptions.

6.2 Strong Exculpability

Recall that strong exculpability allows an honest verifier (or group of verifiers) to prove in a sound fashion that the user with public key $pk_{\mathcal{U}}$ reused an e-token with TSN S.

For strong exculpability, we need to define VerifyViolation and to adapt the Show and the Identify algorithms. In Show", the ZK proof of validity is transformed into a noninteractive proof, denoted Π , using the Fiat-Shamir heuristic [33]. The proof Π is added to the coin transcript, denoted τ . And Identify" $(pk_{\mathcal{I}}, S, \tau_1, \tau_2)$ adds both transcripts τ_1 , and τ_2 to its output $s_{\mathcal{U}}$. (The function $\phi(s_{\mathcal{U}}) = pk_{\mathcal{U}}$ ignores the extra information.)

Thus, the VerifyViolation algorithm is defined as follows: VerifyViolation $(pk_{\mathcal{I}}, S, pk_{\mathcal{U}}, s_{\mathcal{U}})$ parses $\tau_1 = (E_1, R_1, \Pi_1)$ and $\tau_2 = (E_2, R_2, \Pi_2)$ from $s_{\mathcal{U}}$. Then, it checks that $\phi(s_{\mathcal{U}}) = pk_{\mathcal{U}}$ and that Identify" $(pk_{\mathcal{I}}, S, \tau_0, \tau_2) = s_{\mathcal{U}}$. Next, it verifies both non-interactive proofs Π_i with respect to (S, R_i, T_i) . If all checks pass, it accepts; else, it rejects.

A subtlety here is that, for these proofs to be sound even when the issuer is malicious, the group \mathbf{G}' that is needed as a parameter for zero-knowledge proofs here must be a system parameter generated by a trusted third party, such that no one, including the issuer, knows the order of this group. So in particular, \mathbf{G}' cannot be the same as \mathbf{G} [20].

THEOREM 6.2. The above scheme provides strong exculpability under the Strong RSA, and y-DDHI if $l_x \in O(\log k)$ or SDDHI assumptions in the random oracle model with trusted setup for the group \mathbf{G}' .

6.3 Tracing

We can extend our periodic *n*-times authentication scheme so that if a user reuses even one e-token, *all* possible TSN values she could compute using *any* of her dispensers are now publicly computable. We use the same IKeygen', UKeygen', Show', and Identify' algorithms as weak exculpability, slightly modify the Obtain protocol, and define a new Trace algorithm.

In UKeygen', the user's keypair $(\mathbf{e}(g_1, g_2)^{sk_{\mathcal{U}}}, sk_{\mathcal{U}})$ is of the correct form for the bilinear ElGamal cryptosystem, where the value $g_1^{sk_{\mathcal{U}}}$ is sufficient for decryption. Now, in our modified Obtain', the user will provide the issuer with a verifiable encryption [11] of PRF seed *s* under *her own* public key $pk_{\mathcal{U}}$. The issuer stores this tracing information in $R_{\mathcal{U}}$. When Identify' exposes $g_1^{sk_{\mathcal{U}}}$, the issuer may run the following trace algorithm:

 $\begin{aligned} & \mathsf{Trace}(pk_{\mathcal{I}}, pk_{\mathcal{U}}, s_{\mathcal{U}}, R_{\mathcal{U}}, n). \text{ The issuer extracts } g_1^{sk_{\mathcal{U}}} \text{ from } s_{\mathcal{U}}, \\ & \text{and verifies this value against } pk_{\mathcal{U}}; \text{ it aborts on failure. The} \\ & \text{issuer uses } g_1^{sk_{\mathcal{U}}} \text{ to decrypt all values in } R_{\mathcal{U}} \text{ belonging to} \\ & \text{that user, and recovers the PRF seeds for } all \text{ of the user's} \\ & \text{dispensers. For seed } s \text{ and time } t, \text{ all TSNs can be computed} \\ & \text{as } f_s(t,j) = F_{(\mathbf{e}(g_1,g_2),s)}(c(0,t,j)), \text{ for all } 0 \leq j < n. \end{aligned}$

THEOREM 6.3. The above scheme provides tracing of violators under the Strong RSA, y-DDHI if $l_x \in O(\log k)$ or SDDHI, and either XDH or Sum-Free DDH assumptions.

6.4 Dynamic Revocation

Implementing dynamic revocation requires modifying the Obtain and Show protocols in the basic scheme, and defining a new Revoke algorithm.

The mechanisms introduced in [15] can be used for revoking CL signatures. In an adjusted CL protocol for obtaining a signature on a committed value, the user obtains an additional witness $\mathbf{w} = \mathbf{v}^{e^{-1}}$, where \mathbf{v} is the revocation public key and e is a unique prime which is part of the CL signature σ . In the CL protocol for proving knowledge of a signature, the user also proves knowledge of this witness. Violators with prime \tilde{e} can be excluded by updating the revocation public key \mathbf{v} , such that $\mathbf{v}' = \mathbf{v}^{\tilde{e}^{-1}}$, and publishing \tilde{e} . While all non-excluded users can update their witness by computing function $f(e, \tilde{e}, \mathbf{v}', \mathbf{w}) = \mathbf{w}'$, without knowing the order of \mathbf{G} , this update does *not* work when $e = \tilde{e}$.

Thus, our e-token dispensers can be revoked by revoking their CL signature σ . Obtain^{'''} is adapted to provide users with a witness **w** and to store the corresponding *e* as r_D . Show^{'''} is adapted to update and prove knowledge of the witness. The Revoke(pk_T, r_D) algorithm is defined as follows: Compute $\mathbf{v}' = \mathbf{v}^{r_D^{-1}}$ and publish it together with update information r_D . Additional details are in [15].

THEOREM 6.4. The above scheme provides dynamic revocation under the Strong RSA, and y-DDHI if $l_x \in O(\log k)$ or SDDHI assumptions.

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